

Understanding Acoustic Scale Observations

The One Sided Fight Against Λ

Ewan Chamberlain
Supervisor: Antony Lewis

University of Sussex

Monday 07 April 2025

Lewis & Chamberlain, [arxiv:2412.13894](https://arxiv.org/abs/2412.13894)

Understanding Acoustic Scale Observations

The One Sided Fight Against Λ

Ewan Chamberlain
Supervisor: Antony Lewis

University of Sussex

Monday 07 April 2025

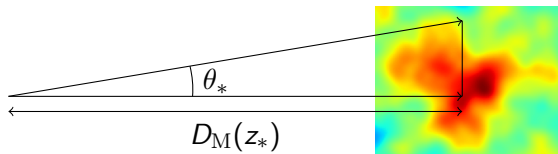
Lewis & Chamberlain, arxiv:2412.13894

Now with DESI DR2!

Outline

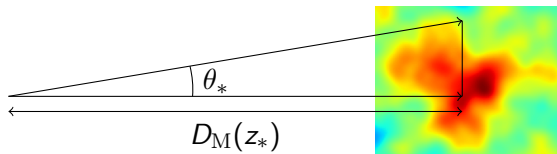
- 1 Background
- 2 Constraints
- 3 Results
- 4 Conclusions

- Cosmic Microwave Background (CMB) and Baryon Acoustic Oscillations (BAO) define “standard rulers”.



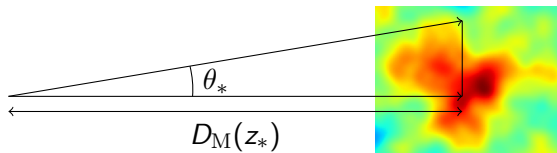
CMB and BAO

- Cosmic Microwave Background (CMB) and Baryon Acoustic Oscillations (BAO) define “standard rulers”.
- CMB constrains the angular size of the sound horizon θ_* .



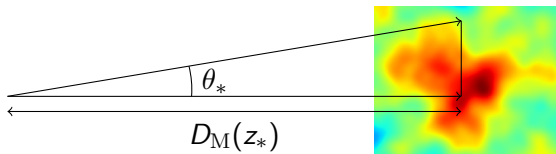
CMB and BAO

- Cosmic Microwave Background (CMB) and Baryon Acoustic Oscillations (BAO) define “standard rulers”.
- CMB constrains the angular size of the sound horizon θ_* .
- Measured to within 0.03% by *Planck*.



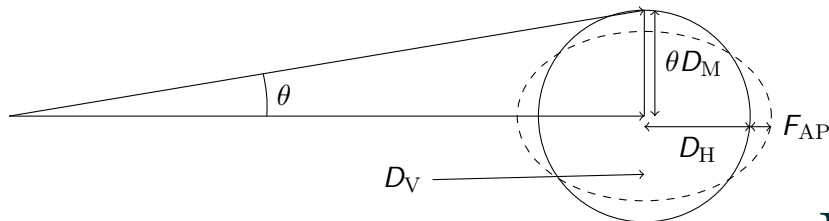
CMB and BAO

- Cosmic Microwave Background (CMB) and Baryon Acoustic Oscillations (BAO) define “standard rulers”.
- CMB constrains the angular size of the sound horizon θ_* .
- Measured to within 0.03% by *Planck*.
- BAO measurements detect lower redshift imprints on galaxies.



BAO Measurements

- Line-of-sight: Hubble distance $D_H(z) = c/H(z)$.
- Transverse: angular diameter distance $D_M(z) = c \int_0^z dz'/H(z')$.
- Angle-averaged BAO scale: $D_V(z) = [z D_M^2(z) D_H(z)]^{1/3}$.
- Alcock-Paczynski parameter: $F_{AP}(z) = D_M(z)/D_H(z)$.



- DESI is testing three dark energy (DE) models: Λ CDM, w CDM, $w_0 w_a$ CDM.

- DESI is testing three dark energy (DE) models: Λ CDM, w CDM, $w_0 w_a$ CDM.
- $w_0 w_a$ CDM (a.k.a. CPL):

$$w(a) = p(a)/\rho(a) = w_0 + w_a(1 - a).$$

- DESI is testing three dark energy (DE) models: Λ CDM, w CDM, $w_0 w_a$ CDM.
- $w_0 w_a$ CDM (a.k.a. CPL):

$$w(a) = p(a)/\rho(a) = w_0 + w_a(1 - a).$$

- $w_0 w_a$ CDM not necessarily consistent with the Null Energy Condition (NEC).

Null Energy Condition

- $\forall k : g_{\mu\nu} k^\mu k^\nu = 0, T_{\mu\nu} k^\mu k^\nu \geq 0$ (arXiv:1401.4024)

Null Energy Condition

- ~~$\forall k : g_{\mu\nu} k^\mu k^\nu = 0, T_{\mu\nu} k^\mu k^\nu \geq 0$ (arXiv:1401.4024)~~
- $p(a) + \rho(a) \geq 0 \implies w(a) \geq -1.$
- “Energy density cannot increase with expansion.”

Null Energy Condition

- ~~$\forall k : g_{\mu\nu} k^\mu k^\nu = 0, T_{\mu\nu} k^\mu k^\nu \geq 0$ (arXiv:1401.4024)~~
- $p(a) + \rho(a) \geq 0 \implies w(a) \geq -1$.
- “Energy density cannot increase with expansion.”
- DESI+CMB+SNe prefers $w_0 w_a$ CDM over Λ CDM.



Null Energy Condition

- $\forall k : \cancel{g_{\mu\nu} k^\mu k^\nu = 0}, \cancel{T_{\mu\nu} k^\mu k^\nu \geq 0}$ (arXiv:1401.4024)
- $p(a) + \rho(a) \geq 0 \implies w(a) \geq -1.$
- “Energy density cannot increase with expansion.”
- DESI+CMB+SNe prefers $w_0 w_a$ CDM over Λ CDM.



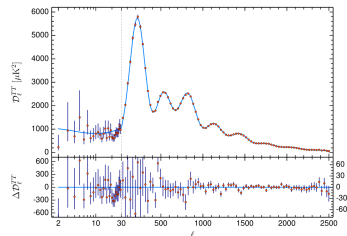
Question

Do DESI measurements imply NEC violation, or is it just an artefact of the model?

Constraints

From *Planck*:

- θ_* is fixed $\implies D_M(z_*)$ is fixed.
- $\Omega_b h^2$ and $\Omega_c h^2$ fixed

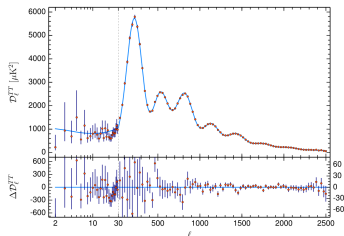


Planck 2018 arXiv:1807.06209

Constraints

From *Planck*:

- θ_* is fixed $\implies D_M(z_*)$ is fixed.
- $\Omega_b h^2$ and $\Omega_c h^2$ fixed



Planck 2018 arXiv:1807.06209

Consider:

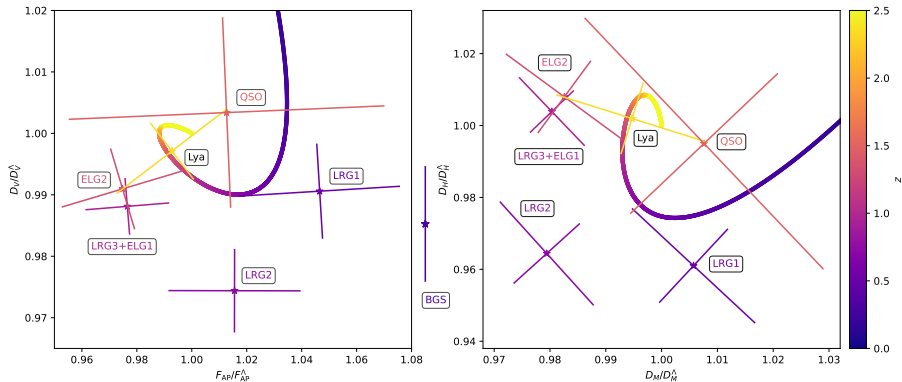
- Null energy condition (NEC) requires that for all fluids $\rho + p = \rho(1 + w) \geq 0 \implies d\rho/dz \geq 0$.

Inequalities

Inequality	Redshift
$D_H(0) \geq D_H^\Lambda(0)$	At $z = 0$
$D_H(z) \geq D_H^\Lambda(z)$	For $0 \leq z \leq z_c$
$D_H(z) \leq D_H^\Lambda(z)$	For $z_c \leq z \leq z_*$
$D_M(z) \geq D_M^\Lambda(z)$	For all z
$\frac{D_H}{D_H^\Lambda} \leq \frac{D_M}{D_M^\Lambda}$	For all z
$F_{AP} \geq F_{AP}^\Lambda$	For all z
$D_V \geq D_V^\Lambda$	For $0 \leq z \leq z_c$
$\frac{D_V}{D_V^\Lambda} \geq \left(\frac{F_{AP}}{F_{AP}^\Lambda} \right)^{-1/3}$	For $z > z_c$

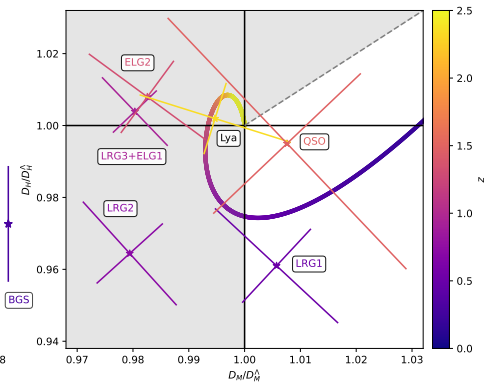
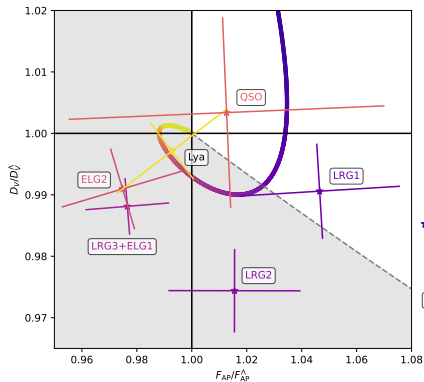
DESI BAO DR2 Measurements

$$w_0 = -0.48, w_a = -1.34$$



DESI BAO DR2 Measurements

$$w_0 = -0.48, w_a = -1.34$$



Conclusions

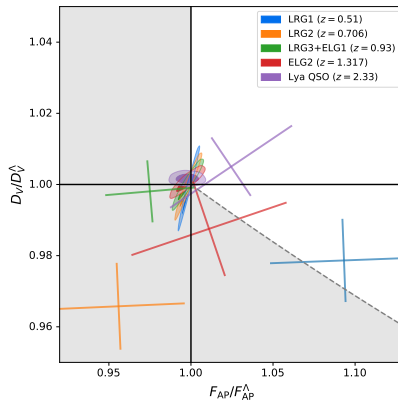
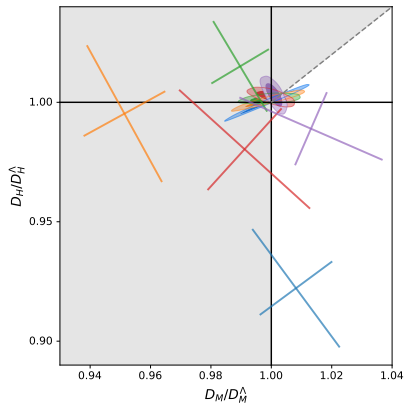
Email: e.a.chamberlain@sussex.ac.uk

Website: ewanchamberlain.github.io

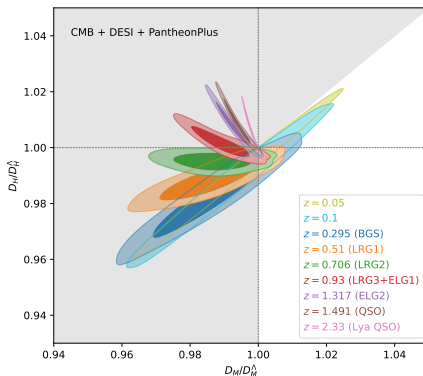
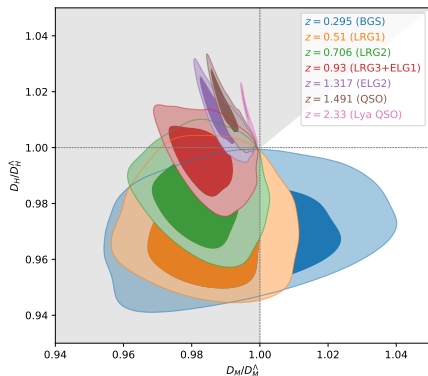
Paper: [arXiv:1807.06209](https://arxiv.org/abs/1807.06209)

- NEC imposes strict conditions on BAO observables relative to Λ CDM.
- These constraints rule out substantial regions of parameter space.
- DESI+CMB measurements exhibit small tensions with Λ CDM that cannot be explained by any NEC-consistent DE model.
- Current acoustic data favour Λ CDM over other NEC-consistent models up to statistical fluctuations.

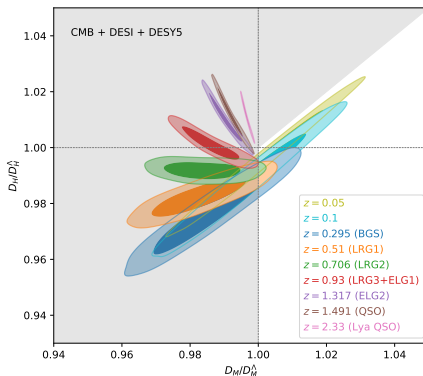
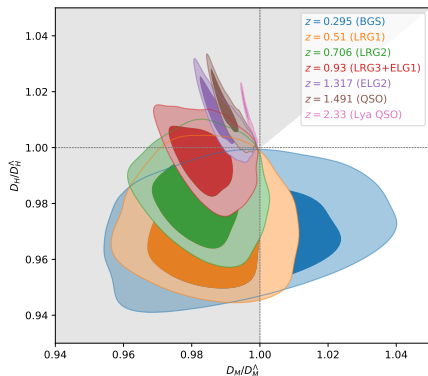




DESI DR1 BAO Measurements + SNe

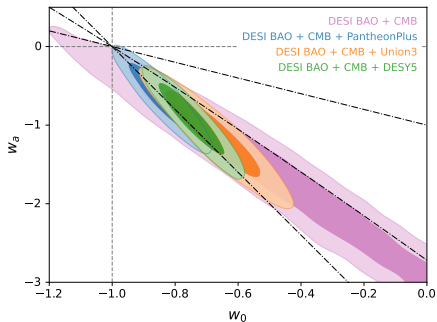


DESI DR1+DESY5



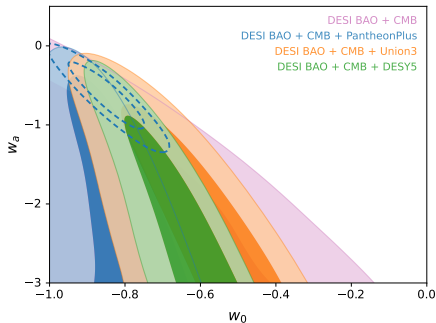
$w_0 w_a$ CDM

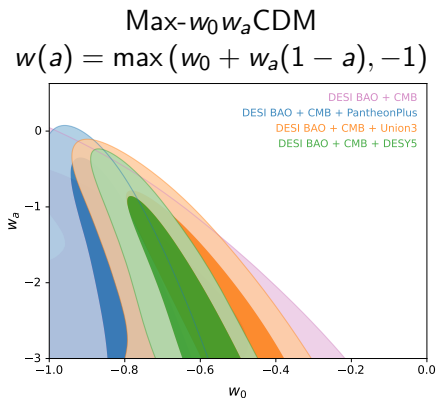
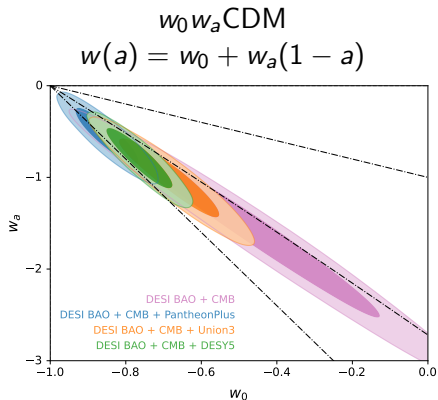
$$w(a) = w_0 + w_a(1 - a)$$



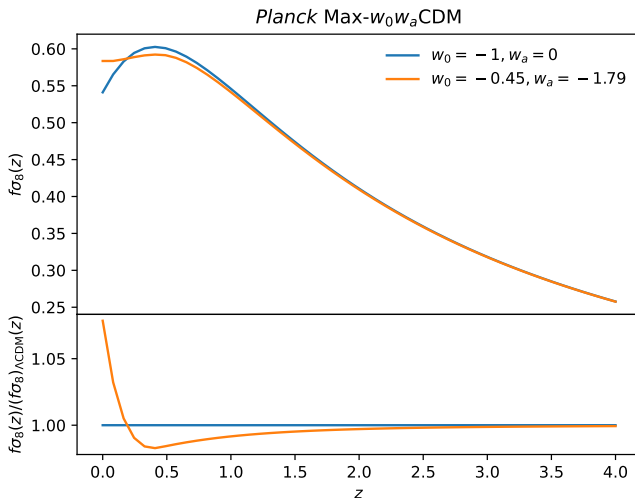
Max- $w_0 w_a$ CDM

$$w(a) = \max(w_0 + w_a(1 - a), -1)$$





Growth of Structure



Hubble Distance

$$D_H(z) \propto \frac{1}{\sqrt{\rho_m(z) + \rho_{de}(z)}},$$

$$\frac{d\rho_{de}}{dz} \geq 0,$$

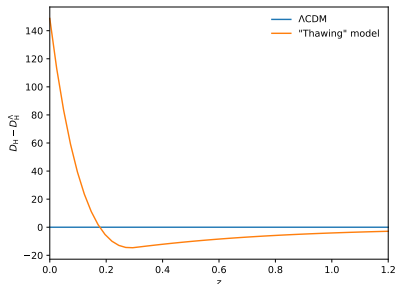
$$\rho_{de}(0) < \rho_\Lambda.$$

Hubble Distance

$$D_H(z) \propto \frac{1}{\sqrt{\rho_m(z) + \rho_{de}(z)}},$$

$$\frac{d\rho_{de}}{dz} \geq 0,$$

$$\rho_{de}(0) < \rho_\Lambda.$$

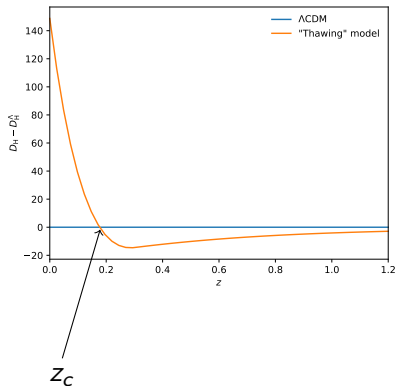


Hubble Distance

$$D_H(z) \propto \frac{1}{\sqrt{\rho_m(z) + \rho_{de}(z)}},$$

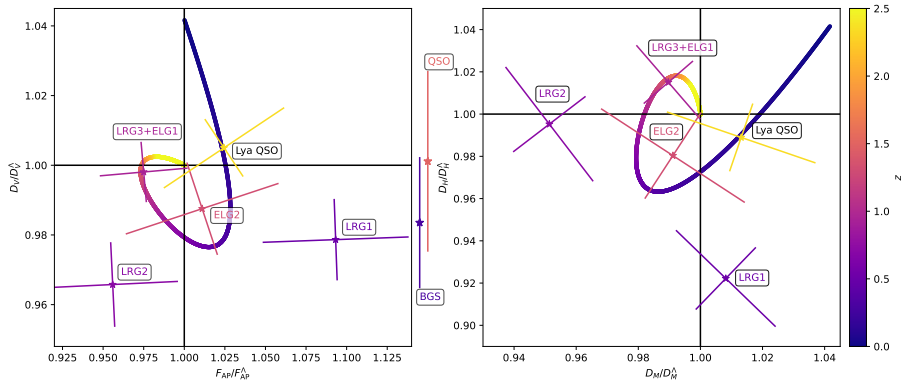
$$\frac{d\rho_{de}}{dz} \geq 0,$$

$$\rho_{de}(0) < \rho_\Lambda.$$



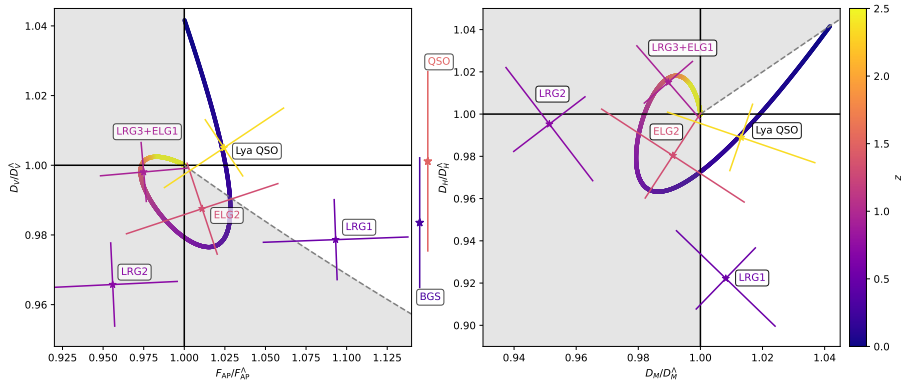
DESI BAO Measurements

$$w_0 = -0.45, w_a = -1.79$$

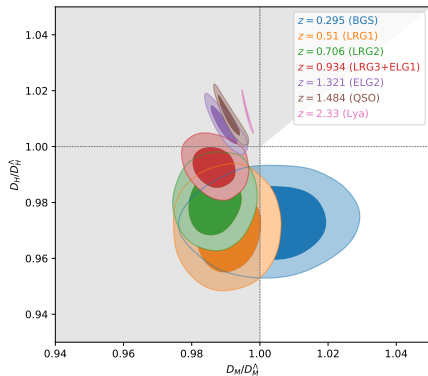


DESI BAO Measurements

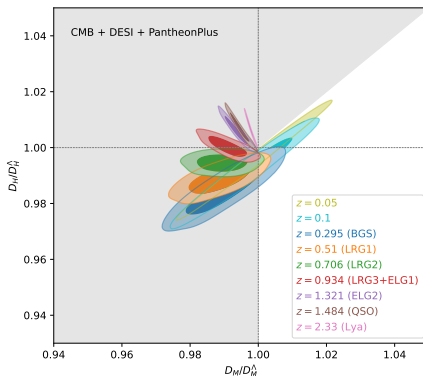
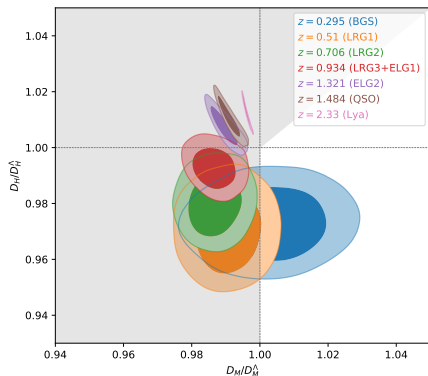
$$w_0 = -0.45, w_a = -1.79$$

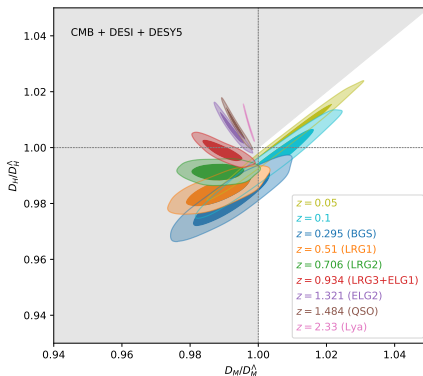
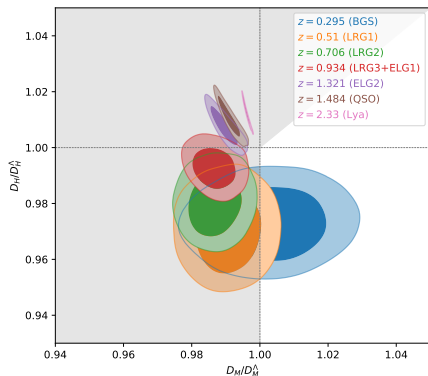


DESI BAO Measurements + SNe



DESI BAO Measurements + SNe





Redshift Bounds

